

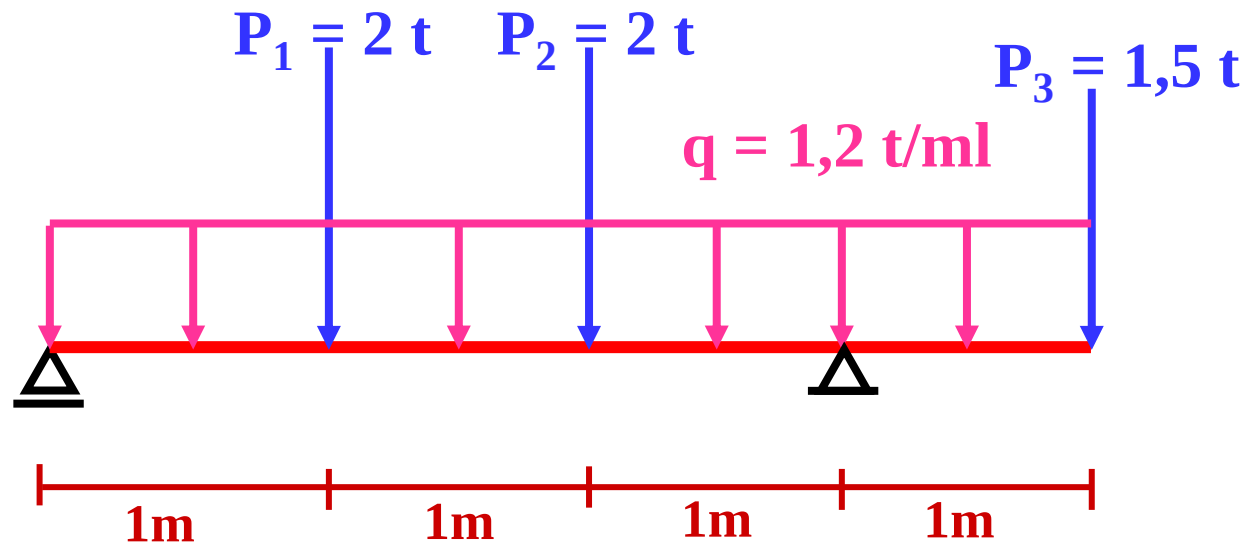


Série N° 04

La flexion simple

Exercice 1

Sachant que la contrainte critique $\sigma_{cr} = 3000 \text{ Kg/cm}^2$, le coefficient de sécurité $C_s = 2$ et la section de la poutre étant carrée ($h=b$).
Calculer la côte (b) de la poutre.



Solution Ex 1

1-Construction du diagramme équivalent des forces et l'établissement des equations d'équilibre, on trouve

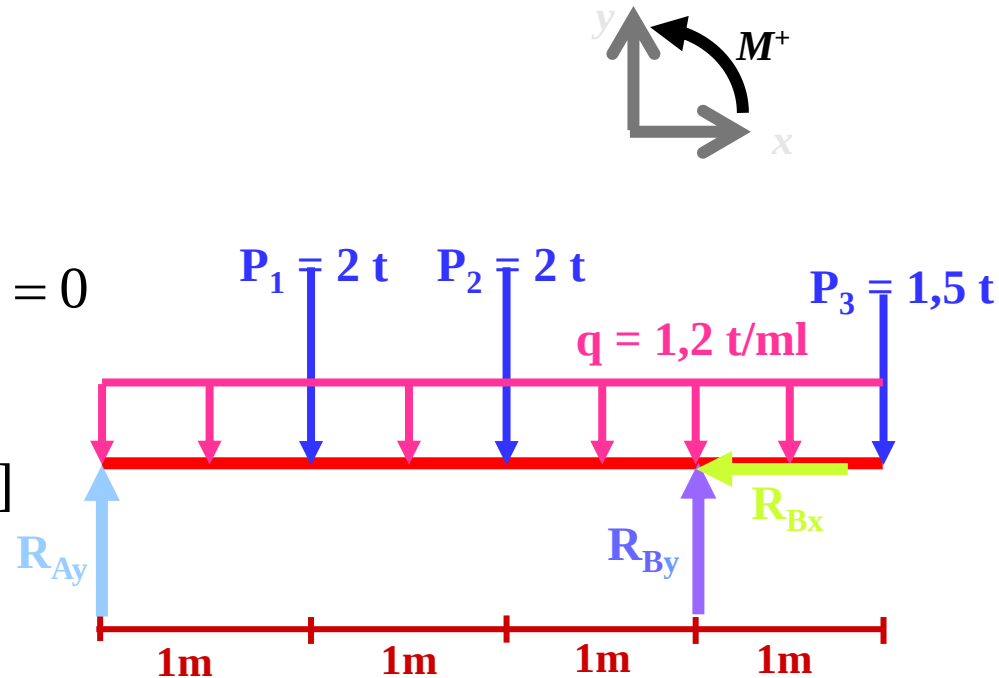
$$\Sigma F_{/x} = 0 \Rightarrow R_{B_x} = 0$$

$$\Sigma F_{/y} = 0 \Rightarrow R_{A_y} + R_{B_y} = 10.3$$

$$\Sigma M_{/A} = 0 \Rightarrow 3R_{B_y} - 2 - 4 - 6 - 9.6 = 0$$

$$\Rightarrow R_{B_y} = 7.2 [t]$$

Donc: $R_{B_y} = 7.2 [t]$; $R_{A_y} = 3.1 [t]$



Solution Ex 1

2-Calcul du moment fléchissant et de l'effort tranchant.

$$0 \leq x < 1m$$

$$T(x) = 3.1 - 1.2x \begin{cases} T(0) = 3.1 [t] \\ T(1) = 1.9 [t] \end{cases}$$

$$M(x) = 3.1x - 1.2 \frac{x^2}{2} \begin{cases} M(0) = 0 \\ M(1) = 2.5 [t.m] \end{cases}$$

$$1 \leq x < 2m$$

$$T(x) = 3.1 - 2 - 1.2 - 1.2(x-1) \begin{cases} T(1) = -0.1 [t] \\ T(2) = -1.3 [t] \end{cases}$$

$$M(x) = 3.1x - 2(x-1) - 1.2(x-0.5) - 1.2 \frac{(x-1)^2}{2} \begin{cases} M(1) = 2.5 [t.m] \\ M(2) = 1.8 [t.m] \end{cases}$$

Solution Ex 1

2-Calcul du moment fléchissant et de l'effort tranchant.

$$2 \leq x < 3m$$

$$T(x) = 3.1 - 2 - 2 - 2.4 - 1.2(x - 2) \begin{cases} T(2) = -3.3[t] \\ T(3) = -4.5[t] \end{cases}$$

$$M(x) = 3.1x - 2(x - 1) - 2(x - 2) - 2.4(x - 1) - 1.2 \frac{(x - 2)^2}{2} \begin{cases} M(2) = 1.8[t.m] \\ M(3) = -2.1[t.m] \end{cases}$$

$$3 \leq x < 4m$$

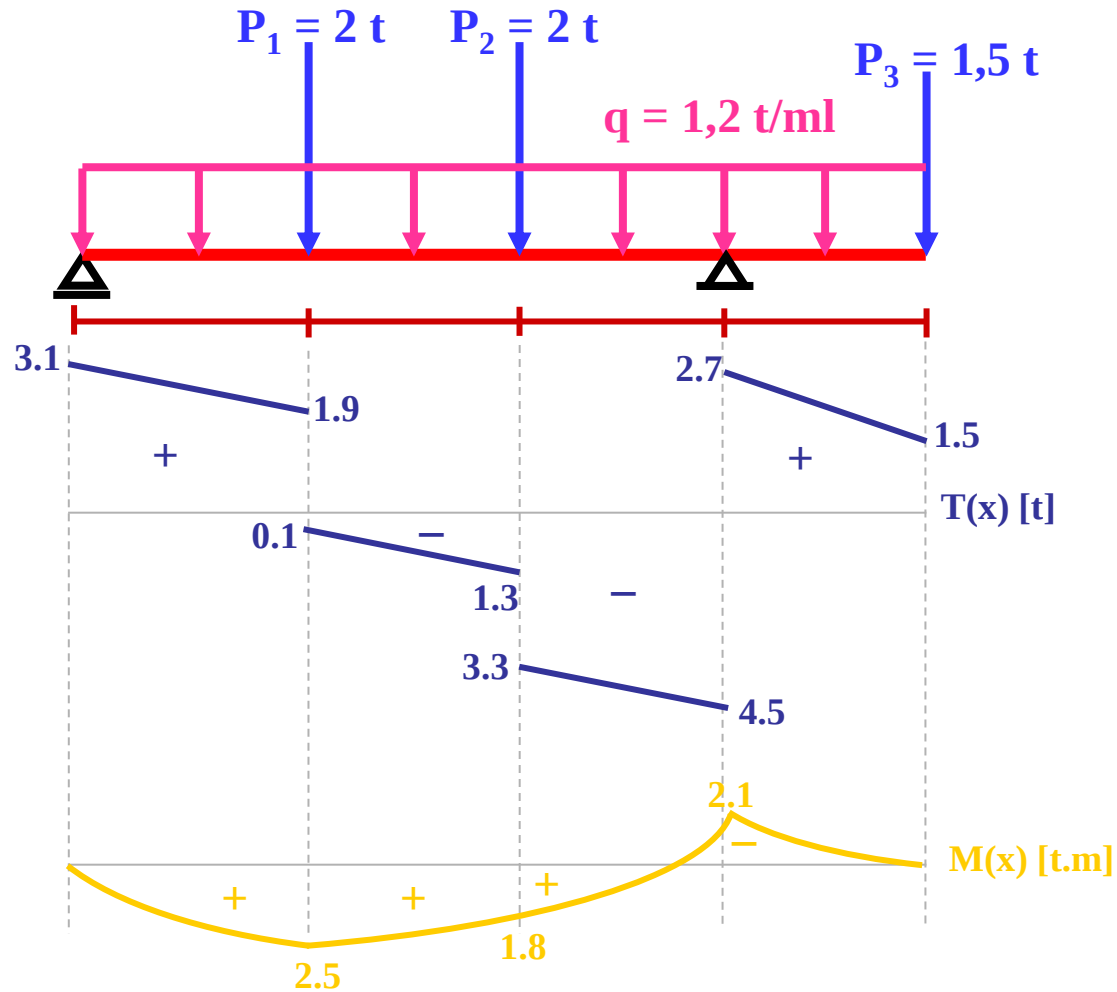
$$T(x) = 3.1 - 2 - 2 + 7.2 - 3.6 - 1.2(x - 3) \begin{cases} T(3) = 2.7[t] \\ T(4) = 1.5[t] \end{cases}$$

$$M(x) = 3.1x - 2(x - 1) - 2(x - 2) + 7.2(x - 3) - 3.6(x - 1.5) - 1.2 \frac{(x - 3)^2}{2}$$

$$\begin{cases} M(3) = -2.1[t.m] \\ M(4) = 0 \end{cases}$$

Solution Ex 1

2-Le tracé du diagramme de $T(x)$ et $M(x)$.





Solution Ex 1

Le moment fléchissant maximal est 2.5 [t.m]. Sachant que :

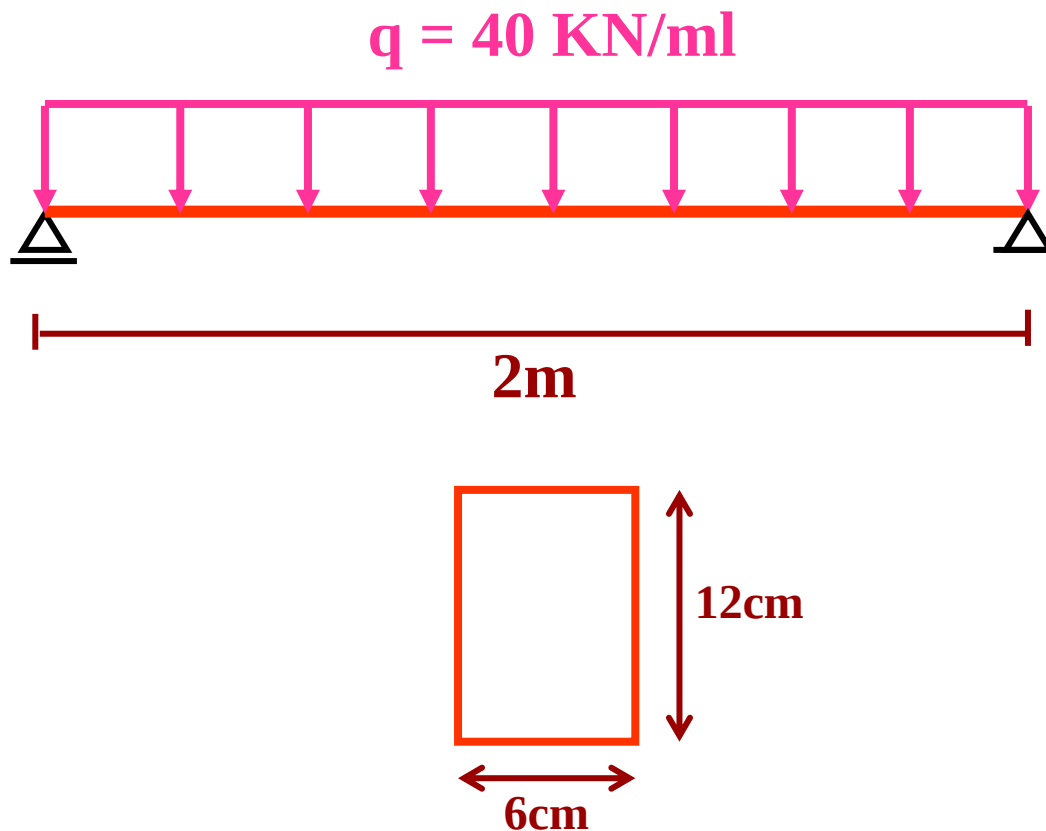
$$h = b; \quad I = \frac{b^4}{12}; \quad y = \frac{b}{2}; \quad \sigma_{adm} = 1500 [Kg / cm^2]$$

$$\sigma = \frac{M}{I} y = \frac{6M}{b^3} \leq \sigma_{adm}$$

$$b \geq \sqrt[3]{\frac{6 \times 2.5 \times 1000 \times 100}{1500}} \Rightarrow b \geq 10 [cm]$$

Exercice 2

Vérifier la résistance de la poutre ci-dessous sachant que la résistance admissible $\sigma_{adm} = 160 \text{ N/mm}^2$.





Solution Ex 2

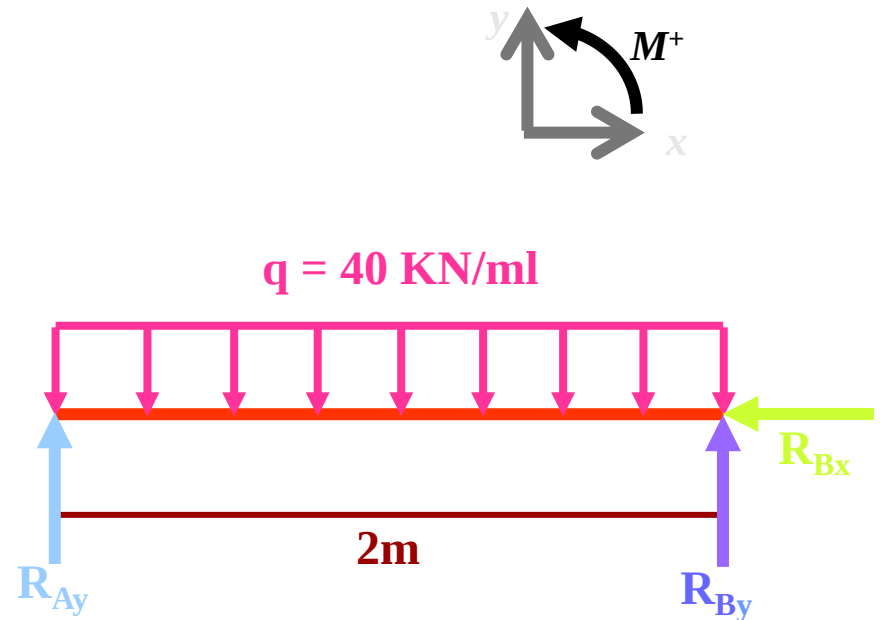
1-Construction du diagramme équivalent des forces et l'établissement des equations d'équilibre, on trouve

$$\Sigma F_{/x} = 0 \Rightarrow R_{B_x} = 0$$

$$\Sigma F_{/y} = 0 \Rightarrow R_{A_y} + R_{B_y} = 80$$

$$\begin{aligned}\Sigma M_{/A} = 0 &\Rightarrow 2R_{B_y} - 80 = 0 \\ &\Rightarrow R_{B_y} = 40 [KN]\end{aligned}$$

$$\text{Donc: } R_{B_y} = 40 [KN]; \quad R_{A_y} = 40 [KN]$$



Solution Ex 2

2-Calcul du moment fléchissant et de l'effort tranchant.

$$0 \leq x < 2m$$

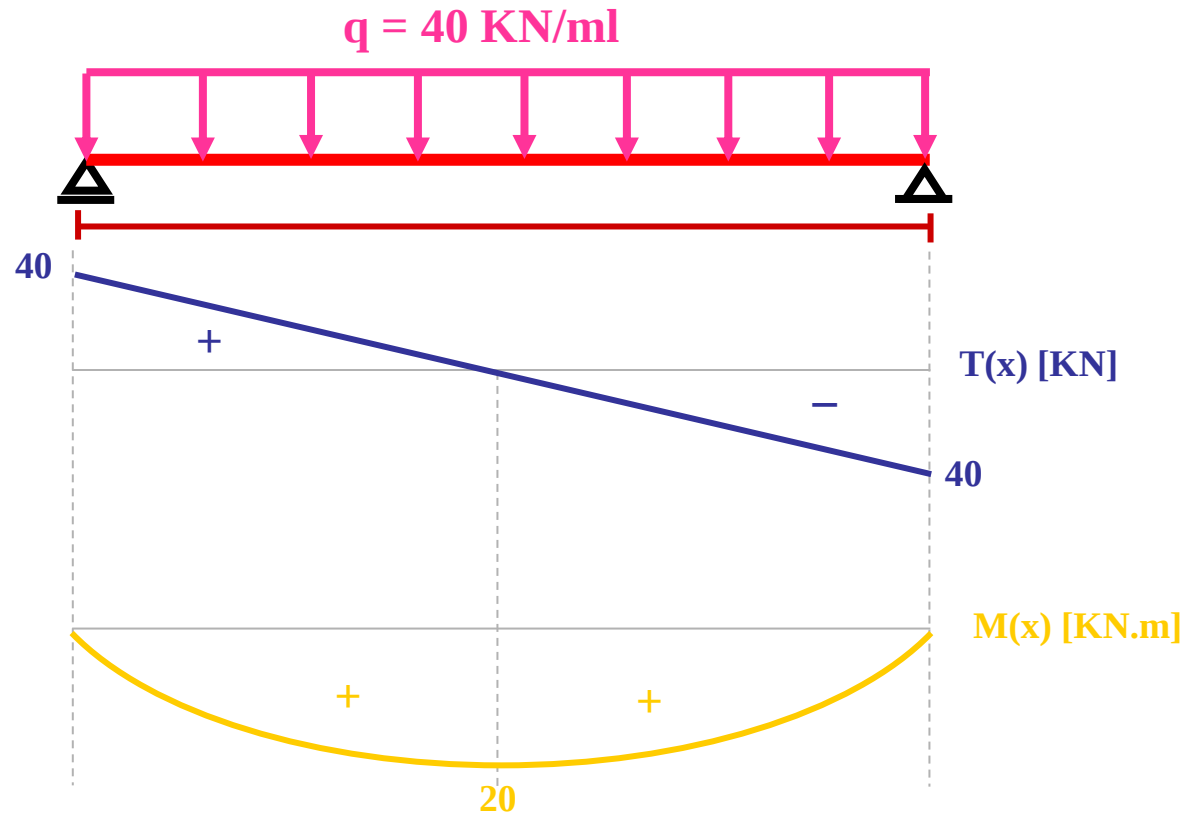
$$T(x) = 40 - 40x \begin{cases} T(0) = 40 [KN] \\ T(2) = -40 [KN] \\ T(x) = 0 \Rightarrow x = 1m \end{cases}$$

$$M(x) = 40x - 40 \frac{x^2}{2} \begin{cases} M(0) = 0 \\ M(2) = 0 \\ M(1) = 20 [KN.m] \end{cases}$$



Solution Ex 2

2-Le tracé du diagramme de $T(x)$ et $M(x)$.



Solution Ex 2

Le moment fléchissant maximal est 20 [KN.m]. Sachant que :

$$I = \frac{hb^3}{12} = \frac{60 \times 120^3}{12}; \quad y = \frac{h}{2}; \quad \sigma_{adm} = 160 [N / mm^2]$$

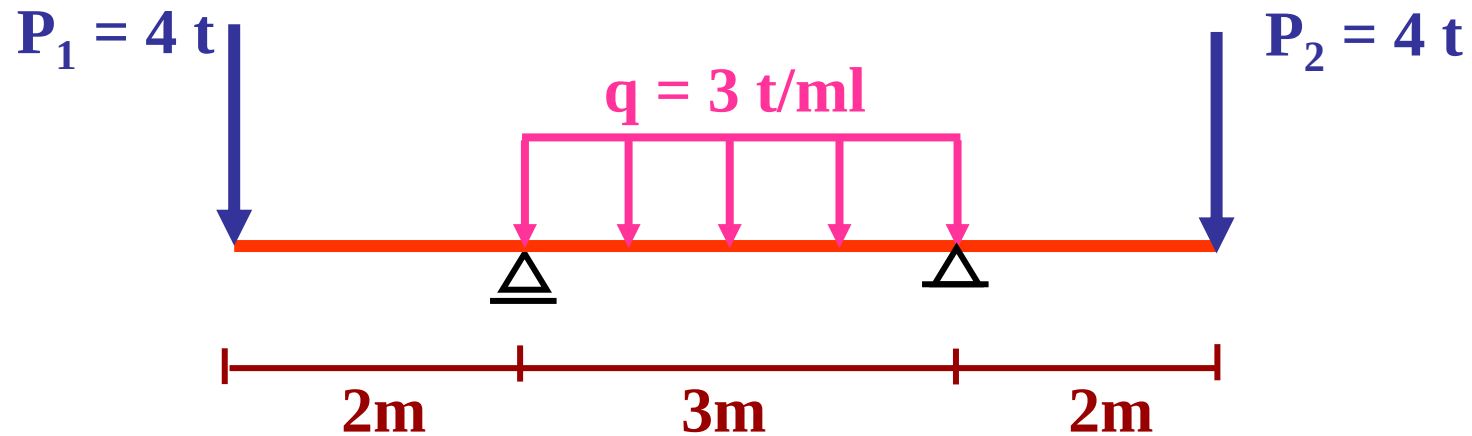
$$\sigma = \frac{M}{I} y \Rightarrow \sigma_{\max} = \frac{20 \times 10^6}{864 \times 10^4} \times 60$$

$$\sigma_{\max} = 138.89 [N / mm^2]$$

$$\sigma_{\max} < \sigma_{adm}$$

Exercice 3

Déterminer le diamètre de la section de la poutre ci-dessous, sachant que $\sigma_{cr} = 3000 \text{ Kg/cm}^2$ et $C_s = 2$.



Solution Ex 3

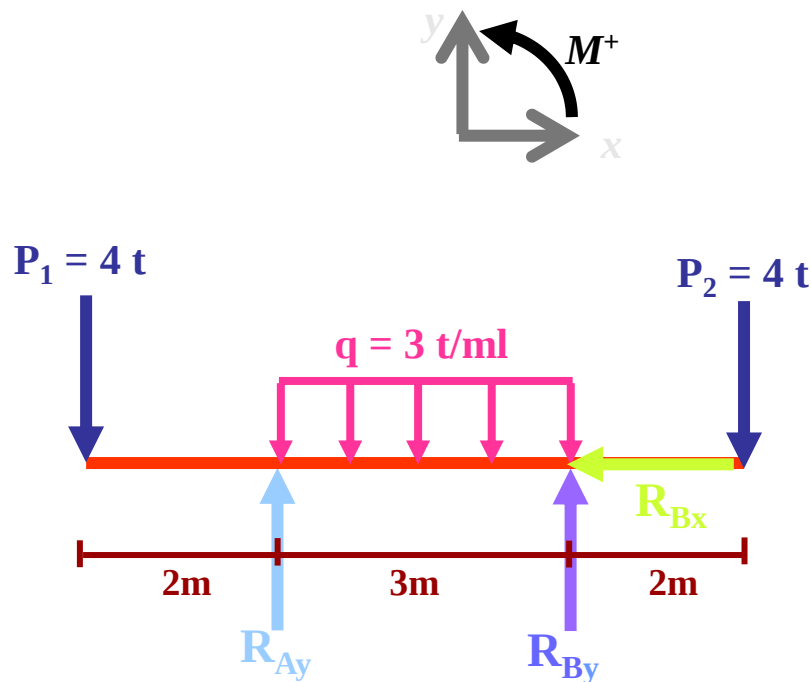
1-Construction du diagramme équivalent des forces et l'établissement des equations d'équilibre, on trouve

$$\Sigma F_{/x} = 0 \Rightarrow R_{B_x} = 0$$

$$\Sigma F_{/y} = 0 \Rightarrow R_{A_y} + R_{B_y} = 17$$

$$\begin{aligned} \Sigma M_{/A} = 0 &\Rightarrow 3R_{B_y} - 25.5 = 0 \\ &\Rightarrow R_{B_y} = 8.5 [t] \end{aligned}$$

$$\text{Donc: } R_{B_y} = 8.5 [t]; \quad R_{A_y} = 8.5 [t]$$



Solution Ex 3

2-Calcul du moment fléchissant et de l'effort tranchant.

$$0 \leq x < 2m$$

$$T(x) = -4$$

$$M(x) = -4x \begin{cases} M(0) = 0 \\ M(2) = -8[t.m] \end{cases}$$

$$2 \leq x < 5m$$

$$T(x) = -4 + 8.5 - 3(x - 2) \begin{cases} T(2) = 4.5[t] \\ T(5) = -4.5[t] \\ T(x) = 0 \Rightarrow x = 3.5m \end{cases}$$

$$M(x) = -4x + 8.5(x - 2) - 3 \frac{(x - 2)^2}{2} \begin{cases} M(2) = -8[t.m] \\ M(5) = -8[t.m] \\ M(3.5) = -4.625[t.m] \end{cases}$$



Solution Ex 3

2-Calcul du moment fléchissant et de l'effort tranchant.

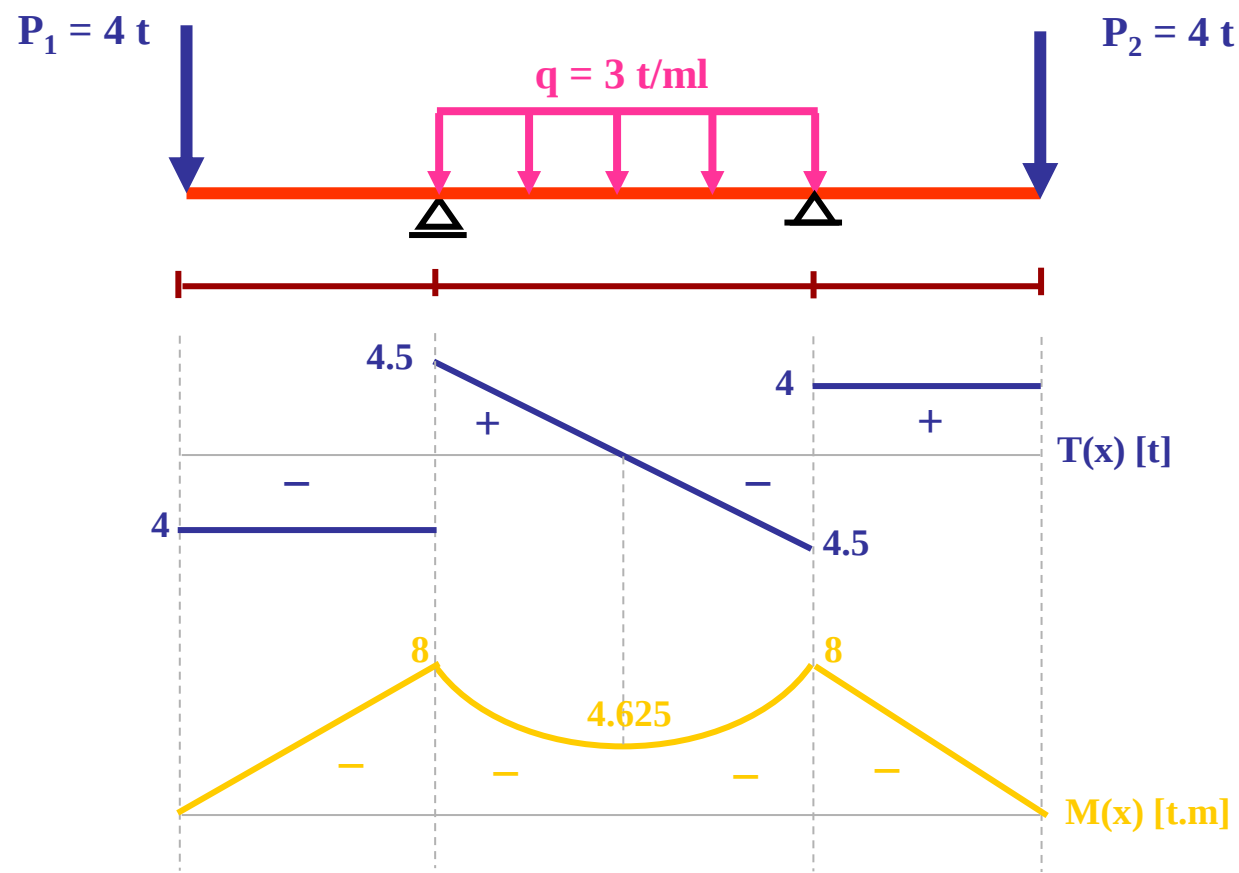
$$5 \leq x < 7m$$

$$T(x) = -4 + 8.5 - 9 + 8.5 = 4$$

$$M(x) = -4x + 8.5(x - 2) - 9(x - 3.5) + 8.5(x - 5) \begin{cases} M(5) = -8 [t.m] \\ M(7) = 0 \end{cases}$$

Solution Ex 3

2-Le tracé du diagramme de T(x) et M(x).





Solution Ex 3

Le moment fléchissant maximal est 8 [t.m]. Sachant que :

$$I = \frac{\pi}{64} D^4; \quad y = \frac{D}{2}; \quad \sigma_{adm} = 1500 [Kg / cm^2]$$

$$\begin{aligned} \sigma = \frac{M}{I} y \leq \sigma_{adm} &\Rightarrow D \geq \sqrt[3]{\frac{32M}{\pi \sigma_{adm}}} \\ &\Rightarrow D \geq \sqrt[3]{\frac{32 \times 8 \times 10^5}{\pi \times 1500}} \\ &\Rightarrow D \geq 17.56 [cm] \end{aligned}$$

Merci

